



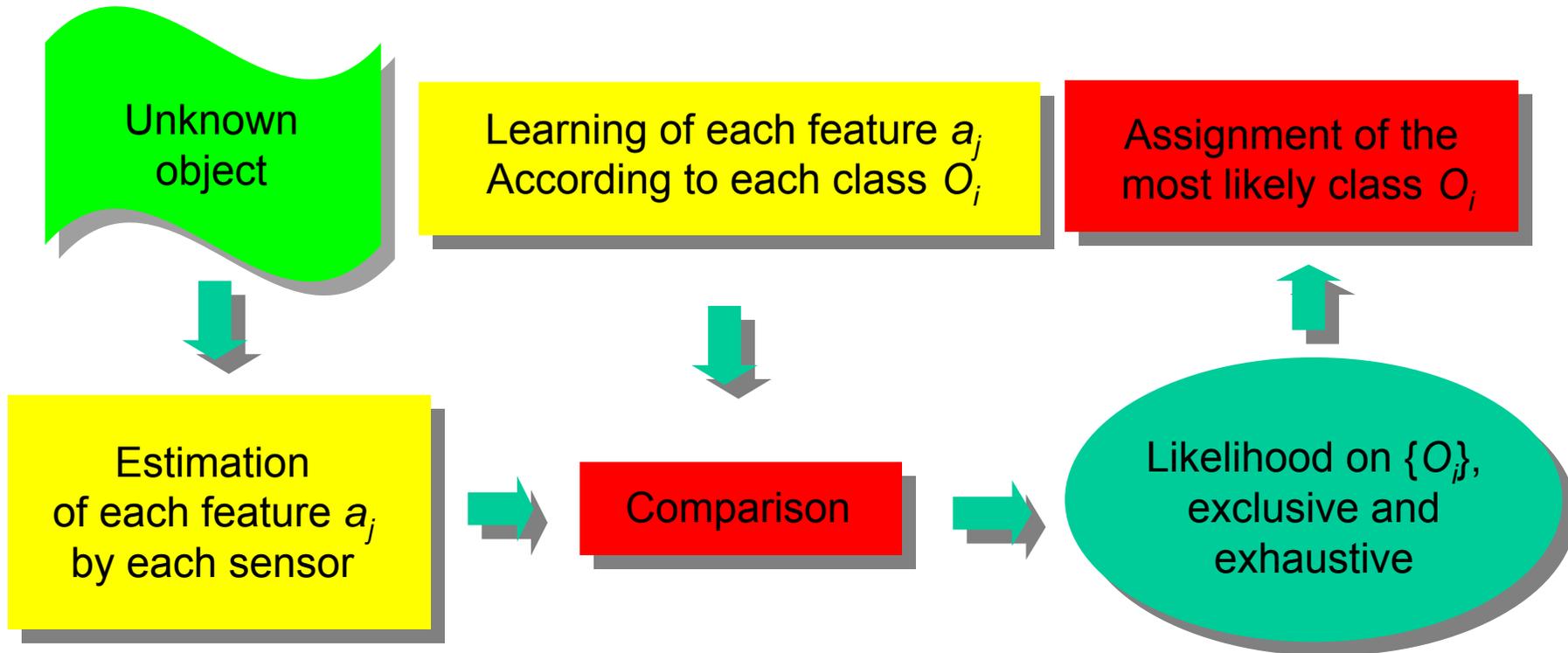
Knowledge Propagation in Information Fusion Processes

Alain APPRIOU



r e t u r n o n i n n o v a t i o n

Classical Classification Process



Further Needs in Classification

Independent assessment of a variety of properties H_i about an unknown object by the sensors, eventually at different times

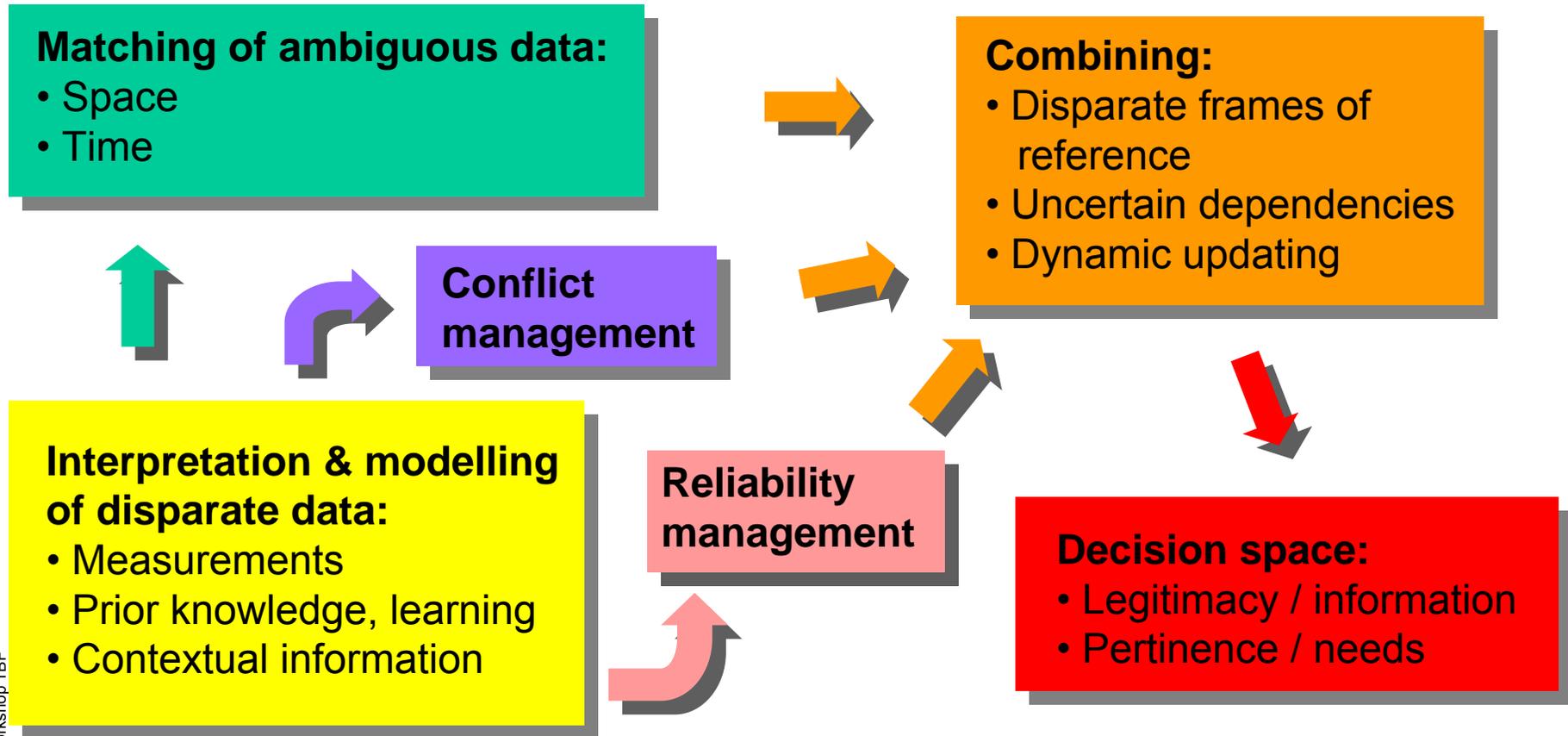
Likelihoods on $\{H_i, \neg H_i\}$

Transposition at a same time & combination

Selection of a set of classes that most likely includes the right one

Likelihood on $\{O_j\}$, exclusive & exhaustive

Frames of Reference in Fusion Processes



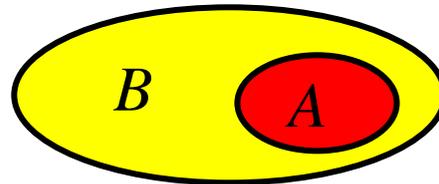
Foundations

Frame of discernment : $E = \{H_i\}, i \in [1, I]$ Exclusive, exhaustive

Mass function : $2^E \rightarrow [0,1]$, $\sum_{A \subseteq E} m(A) = 1$, $m(\emptyset) = 0$

Belief function : minimum likelihood

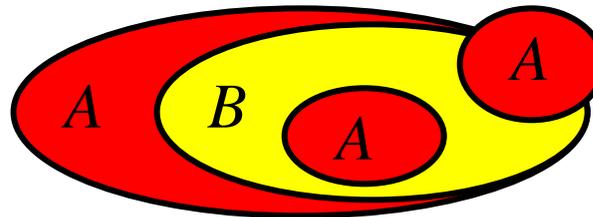
$$Bel(B) = \sum_{A \subseteq B} m(A)$$



Plausibility function : maximum likelihood

$$Pl(B) = \sum_{A \cap B \neq \emptyset} m(A)$$

$$Pl(B) = 1 - Bel(\neg B)$$



Focal element :

$A \subseteq E,$
such that $m(A) \neq 0$

Conditioning - Deconditioning

Conditioning

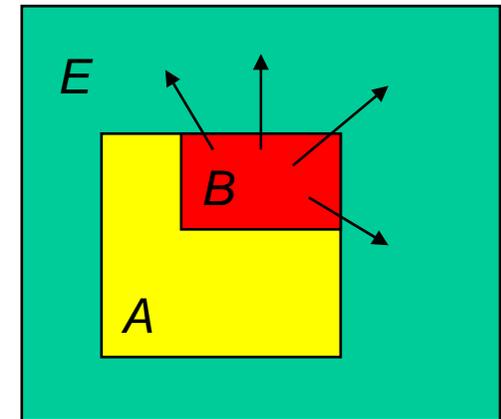
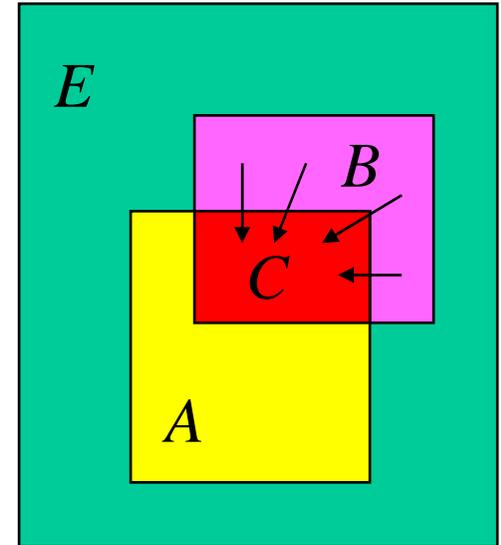
$$\left. \begin{array}{l} m(.) \text{ on } E \\ A \text{ certain, } A \subset E \end{array} \right\} \Rightarrow m(C/A) = \frac{\sum_{B \cap A = C} m(B)}{\sum_{B \cap A \neq \emptyset} m(B)}$$

$$Pl(B/A) = \frac{Pl(B \cap A)}{Pl(A)}$$

Deconditioning

$$\left. \begin{array}{l} \forall B \subseteq A, Pl(B) = \underbrace{Pl(B/A) Pl(A)}_{?} \\ \forall B \not\subseteq A, Pl(B) = ? \end{array} \right\} \Rightarrow \text{Minimal commitment}$$

$$\forall B \subseteq A, m(B \cup \neg A) = m(B/A)$$



Refinement - Coarsening

$$E^1 = \{H_1^1, \dots, H_{I1}^1\} \xrightarrow{R} E^2 = \{H_1^2, \dots, H_{I2}^2\}$$

$$\{R(H_1^1), \dots, R(H_{I1}^1)\} = \text{Partition of } E^2$$

Refinement:

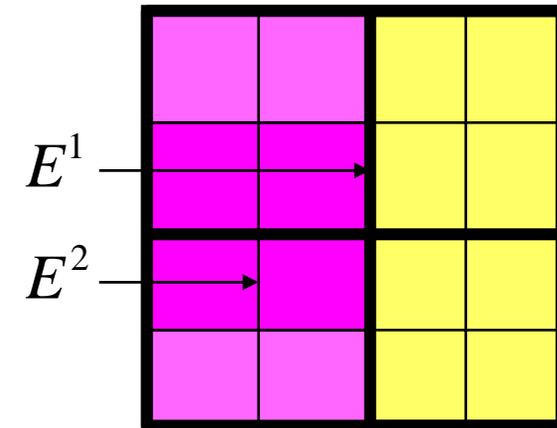
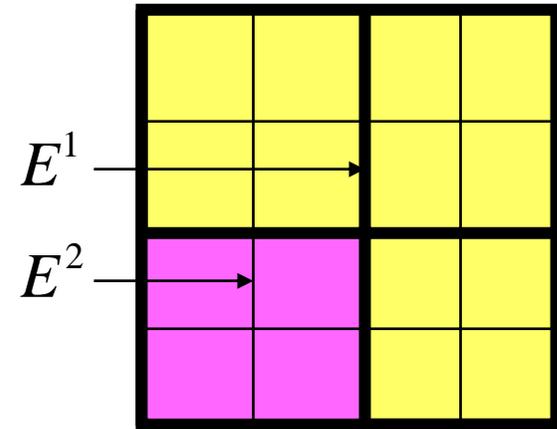
$$m^1(\cdot) \text{ on } E^1 \xrightarrow{R} m^2(\cdot) \text{ on } E^2$$

$$\forall A \subseteq E^1, \quad m^2(R(A)) = m^1(A)$$

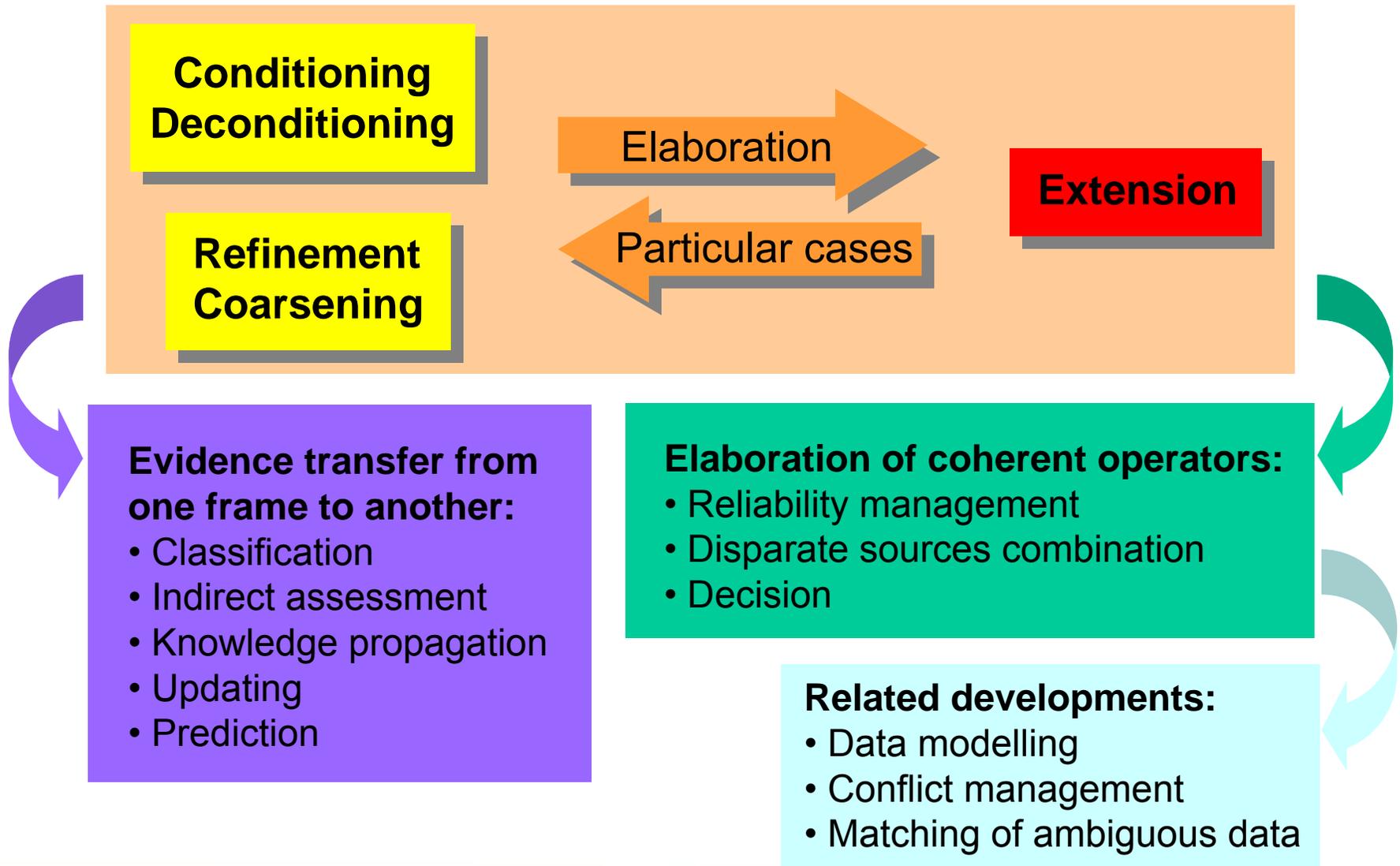
Coarsening:

$$m^2(\cdot) \text{ on } E^2 \xrightarrow{R^{-1}} m^1(\cdot) \text{ on } E^1$$

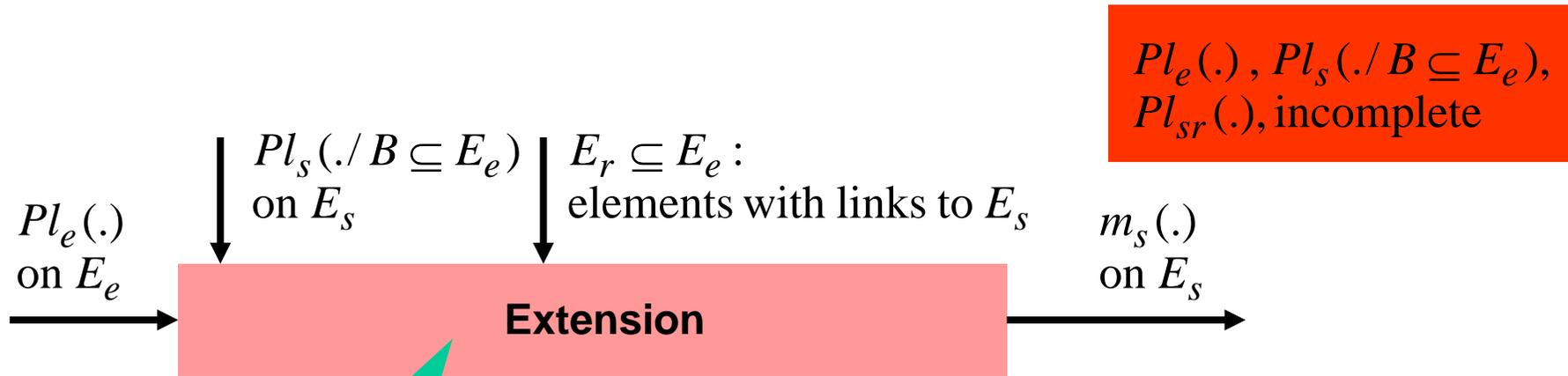
$$m^1(A) = \sum_{\substack{B \subseteq E^2 \\ A = \{H_i^1 / R(H_i^1) \cap B \neq \emptyset\}}} m^2(B)$$



A Federative Approach



Management of Disparate Frames of Discernment and Dependencies



1 $Pl_{sr}(A \times B) = \frac{Pl_s(A / B \subseteq E_r) Pl_e(B)}{Pl_e(E_r)}$ on $E_s \times E_r$

2 $m_{sr}(\cdot)$ of minimal commitment on $E_s \times E_r$ with respect to $Pl_{sr}(\cdot)$

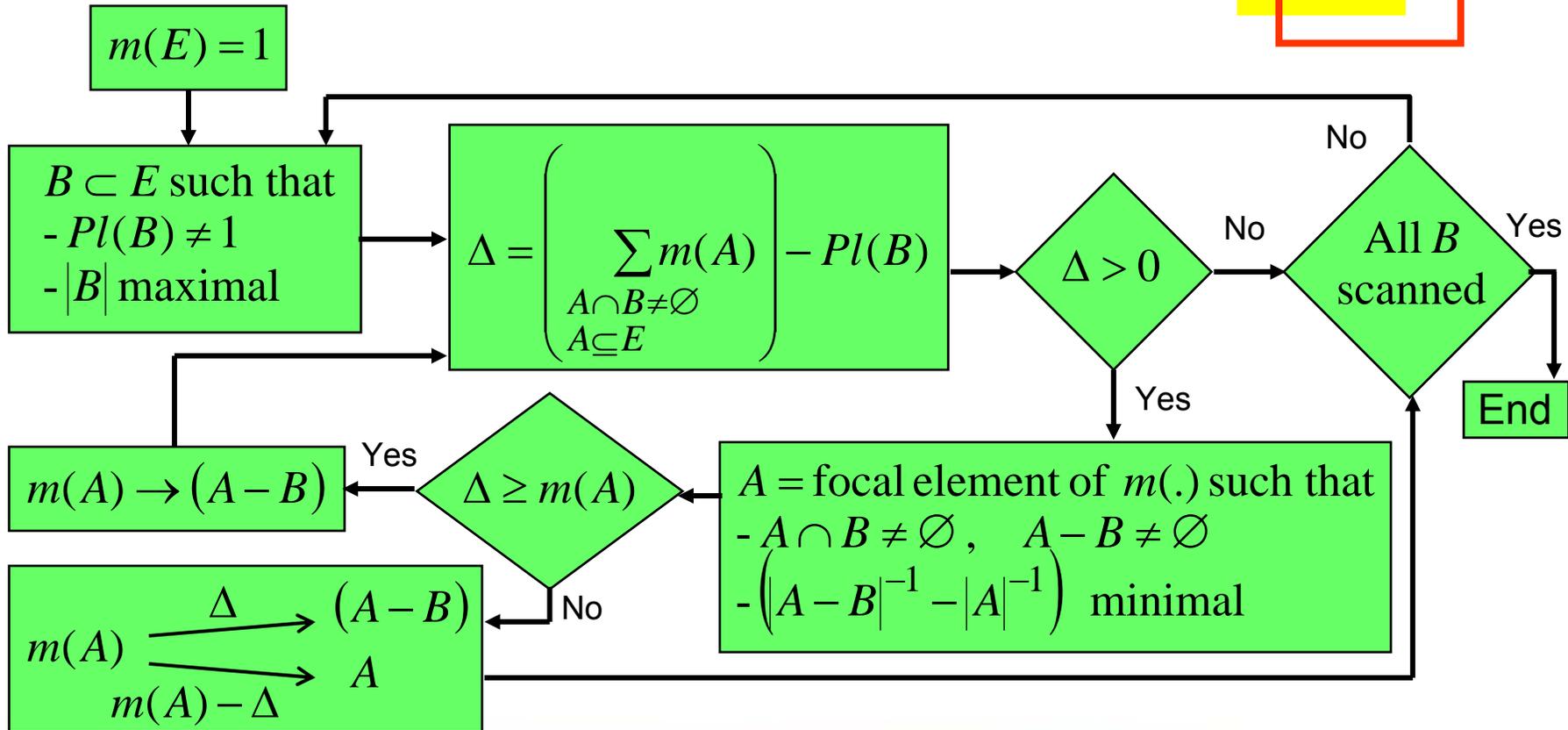
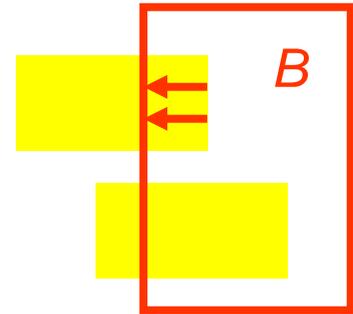
3 Coarsening from $E_s \times E_r$ to E_s :

$$m_s(A) = \sum_{B \subseteq E_r} m_{sr}(A \times B)$$

Determination of $m(\cdot)$ with Minimal Commitment

Incomplete $Pl(\cdot)$ on E \rightarrow Complete $m(\cdot)$ minimizing

$$Sp(m) = \sum_{A \subseteq E} \frac{m(A)}{|A|}$$



Example

Input

$$Pl(H_2 \cup H_3) = 0.6$$

$$Pl(H_1 \cup H_2) = 0.9$$

$$Pl(H_2) = 0.3$$

$$Pl(H_1) = 0.8$$

$$m(E) = 1$$

$$E = \{H_1, H_2, H_3\}$$

$$m(E) = 0.6$$
$$m(H_1) = 0.4$$

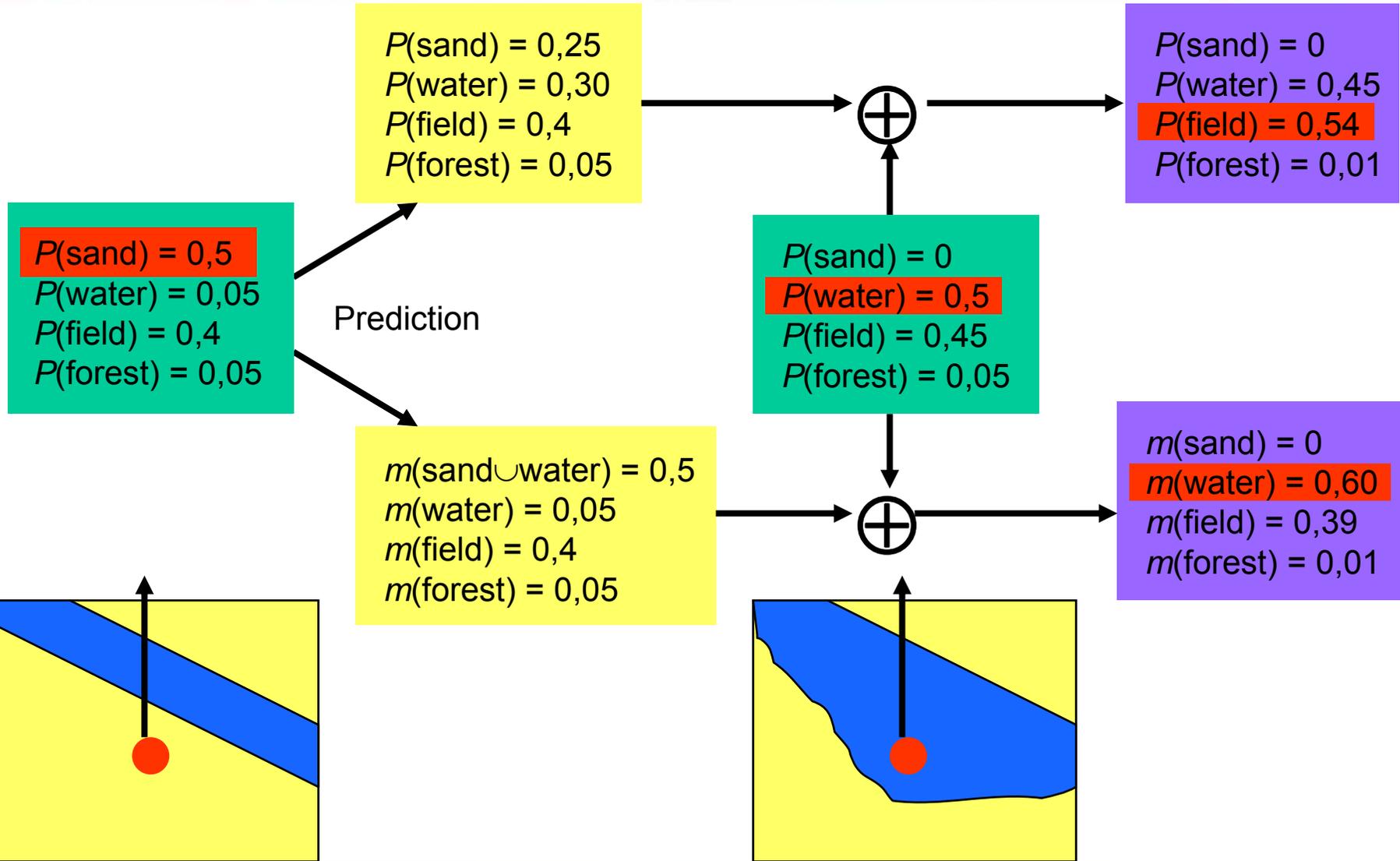
$$m(E) = 0.5$$
$$m(H_1) = 0.4$$
$$m(H_3) = 0.1$$

$$m(E) = 0.3$$
$$m(H_1 \cup H_3) = 0.2$$
$$m(H_1) = 0.4$$
$$m(H_3) = 0.1$$

$$m(E) = 0.2$$
$$m(H_1 \cup H_3) = 0.2$$
$$m(H_2 \cup H_3) = 0.1$$
$$m(H_1) = 0.4$$
$$m(H_3) = 0.1$$

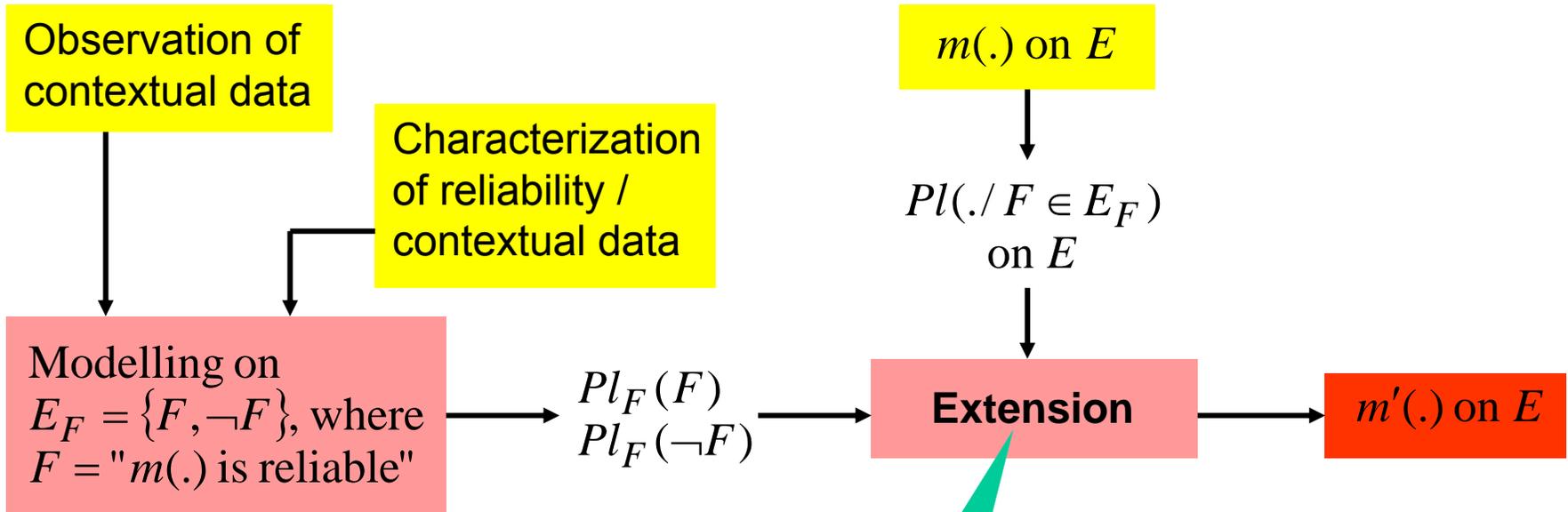
Unique solution

Multidate Image Classification



A. Appriou - Workshop TBF

Reliability Management



- Optimal solution if $m_F(.)$ Bayesian ($m_{sr}(.)$ of minimal commitment)
- Suitable but suboptimal solution otherwise

Discounting $(1 - Pl_F(F))$:
 $m'(A) = Pl_F(F) m(A) \quad \forall A \subset E$
 $m'(E) = 1 - Pl_F(F) (1 - m(E))$

Pixel Classification in Multispectral Images

2 IR sensors : 2 - 2,3 μm , 0,4 - 0,6 μm

2 hypotheses : Asphalt, Vegetation

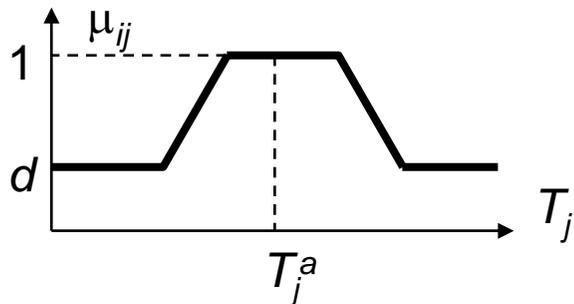
1 contextual variable / sensor j :

water vapor transmittance T_j

Learning in summer :

$$p_a(s_j / H_i, T_j^a)$$

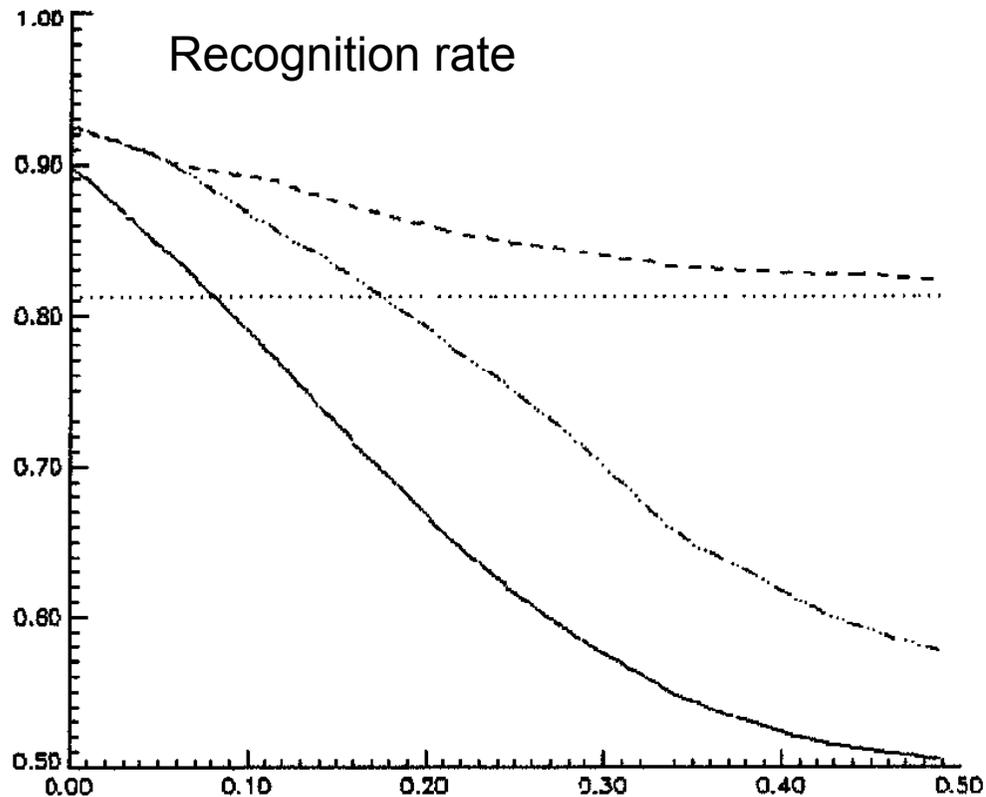
Validity Domain / sensor j :



Real data in winter

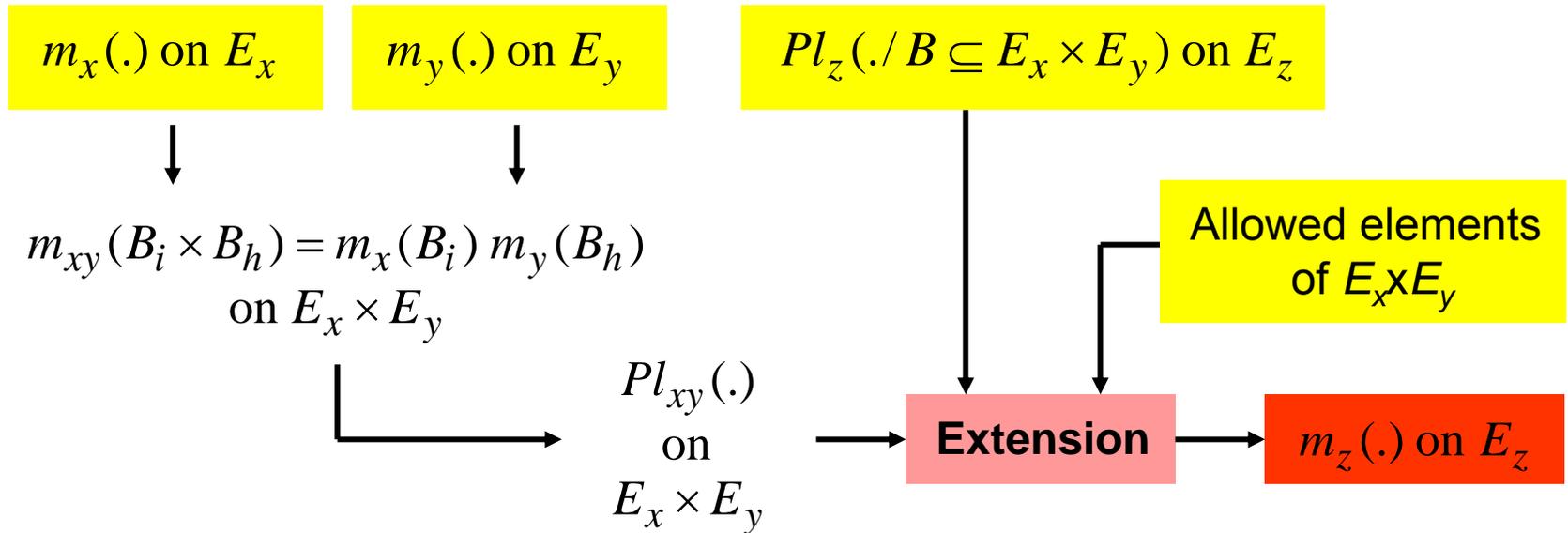
Transmittance observation : T_j^m

- - - - - Probability
 - - - - - TE with reliability management
 ——— Sensor 1
 Sensor 2



T_1^m decreases from T_1^a to 0

Disparate Source Combination



Definition of :

- Particular relations between E_x, E_y , and E_z
- $Pl_z(\cdot / B \subseteq E_x \times E_y)$
- Allowed elements of $E_x \times E_y$



Particular rules of combination

Examples of Particular Rules of Combination

$$E_x = E_y = E_z$$

$Pl_z(A/B_i \times B_h \subseteq E_x \times E_y) = 1$ if it "covers" at least one allowed link
 $Pl_z(A/B_i \times B_h \subseteq E_x \times E_y) = 0$ otherwise

Combination Rule	Allowed Links	Allowed elements
Orthogonal Sum	$B_i \times B_h \rightarrow A = B_i \cap B_h$	$(X_i, Y_h), X_i = Y_h$
Disjunction	$B_i \times B_h \rightarrow A = B_i \cup B_h$	$E_x \times E_y$
Dubois & Prade	$B_i \times B_h \rightarrow A = B_i \cap B_h$, if $B_i \cap B_h \neq \emptyset$ $B_i \times B_h \rightarrow A = B_i \cup B_h$, if $B_i \cap B_h = \emptyset$	$E_x \times E_y$
Yager	$B_i \times B_h \rightarrow A = B_i \cap B_h$, if $B_i \cap B_h \neq \emptyset$ $B_i \times B_h \rightarrow E_z$, if $B_i \cap B_h = \emptyset$	$E_x \times E_y$



Information management



Conflict management

Conflict



Modelling & interpretation according to axioms
 Specific combination rule, to exploit available information

Synthesis of Binary Estimations

Discrimination on $E = \{H_1, \dots, H_i, \dots, H_N\}$

$N \times (N-1)/2$ sources S_{ij}
each on $E_{ij} = \{H_i, H_j\}$



Combination of one-to-one comparisons:

$$P_{ij}(H_i) + P_{ij}(H_j) + P_{ij}(ign.) = 1$$

$$i \in [1, N-1], \quad j \in [i+1, N]$$

$$Pl \left(A \subseteq E / B = \{H^k\} \subseteq \prod_{S_{ij} \in S} E_{ij} \right)$$

$$= 1 \quad \text{if } \exists H_i \in A, H^{ij} = H_i \quad \forall j$$

$$= 0 \quad \text{otherwise}$$

Allowed elements H^k of $\prod_{S_{ij}} E_{ij}$:

$$H^k = (H^{12}, \dots, H^{ij}, \dots), H^{ij} \in E_{ij}$$

such that : $\exists H_i \in E, H^{ij} = H_i, \forall j$

$$m_{ij}(H_i) = P_{ij}(H_i)$$

$$m_{ij}(H_j) = P_{ij}(H_j)$$

$$m_{ij}(E_{ij}) = P_{ij}(ind.)$$

Combination
with respect
to i & j

$$Pl(H_i) = \frac{\prod_{\substack{j \in [1, N] \\ j \neq i}} [P_{i,j}(H_i) + P_{i,j}(ind.)]}{1 - K}$$

Fusion of Binary Classifiers

$Pl(A/B \subseteq E_{12} \times E_{23} \times E_{31}) = 1$ if it "covers":
 either : $(H_1, H_j, H_1) \rightarrow H_1$
 or : $(H_2, H_2, H_j) \rightarrow H_2$
 or : $(H_j, H_3, H_3) \rightarrow H_3$
 $Pl(A/B \subseteq E_{12} \times E_{23} \times E_{31}) = 0$ otherwise

Allowed elements :
 (H_1, H_j, H_1)
 (H_2, H_2, H_j)
 (H_j, H_3, H_3)

$E_{12} = \{H_1, H_2\}$
 $m_{12}(H_1) = 0,4$
 $m_{12}(H_2) = 0,6$

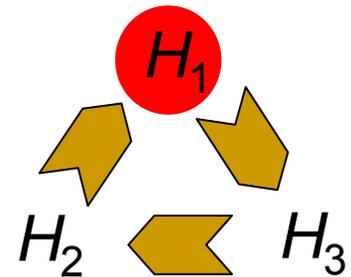
$E_{23} = \{H_2, H_3\}$
 $m_{23}(H_2) = 0,3$
 $m_{23}(H_3) = 0,7$

$E_{31} = \{H_3, H_1\}$
 $m_{31}(H_3) = 0,3$
 $m_{31}(H_1) = 0,7$

Combination

$E = \{H_1, H_2, H_3\}$
 $m(H_1) = 0,42$
 $m(H_2) = 0,27$
 $m(H_3) = 0,31$

$S_{ij} \rightarrow$ Discrimination between H_i et H_j
 Distance / learning $\rightarrow P_{ij}(H_i) + P_{ij}(H_j) = 1$



Combination of Preferences in Multicriteria Decision

$Pl(A/B \subseteq E_{12} \times E_{23} \times E_{31}) = 1$ if it "covers":
 either : $(H_1, H_j, H_1) \rightarrow H_1$
 or : $(H_2, H_2, H_j) \rightarrow H_2$
 or : $(H_j, H_3, H_3) \rightarrow H_3$
 $Pl(A/B \subseteq E_{12} \times E_{23} \times E_{31}) = 0$ otherwise

Allowed elements :
 (H_1, H_j, H_1)
 (H_2, H_2, H_j)
 (H_j, H_3, H_3)

$E_{12} = \{H_1, H_2\}$
 $m_{12}(H_1) = 0,2$
 $m_{12}(H_2) = 0,5$
 $m_{12}(E_{ij}) = 0,3$

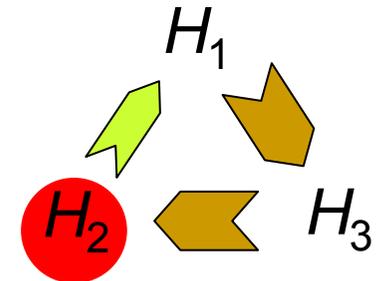
Combination

$E = \{H_1, H_2, H_3\}$
 $Pl(H_1) \cong 0,30$
 $Pl(H_2) \cong 0,32$
 $Pl(H_3) \cong 0,24$

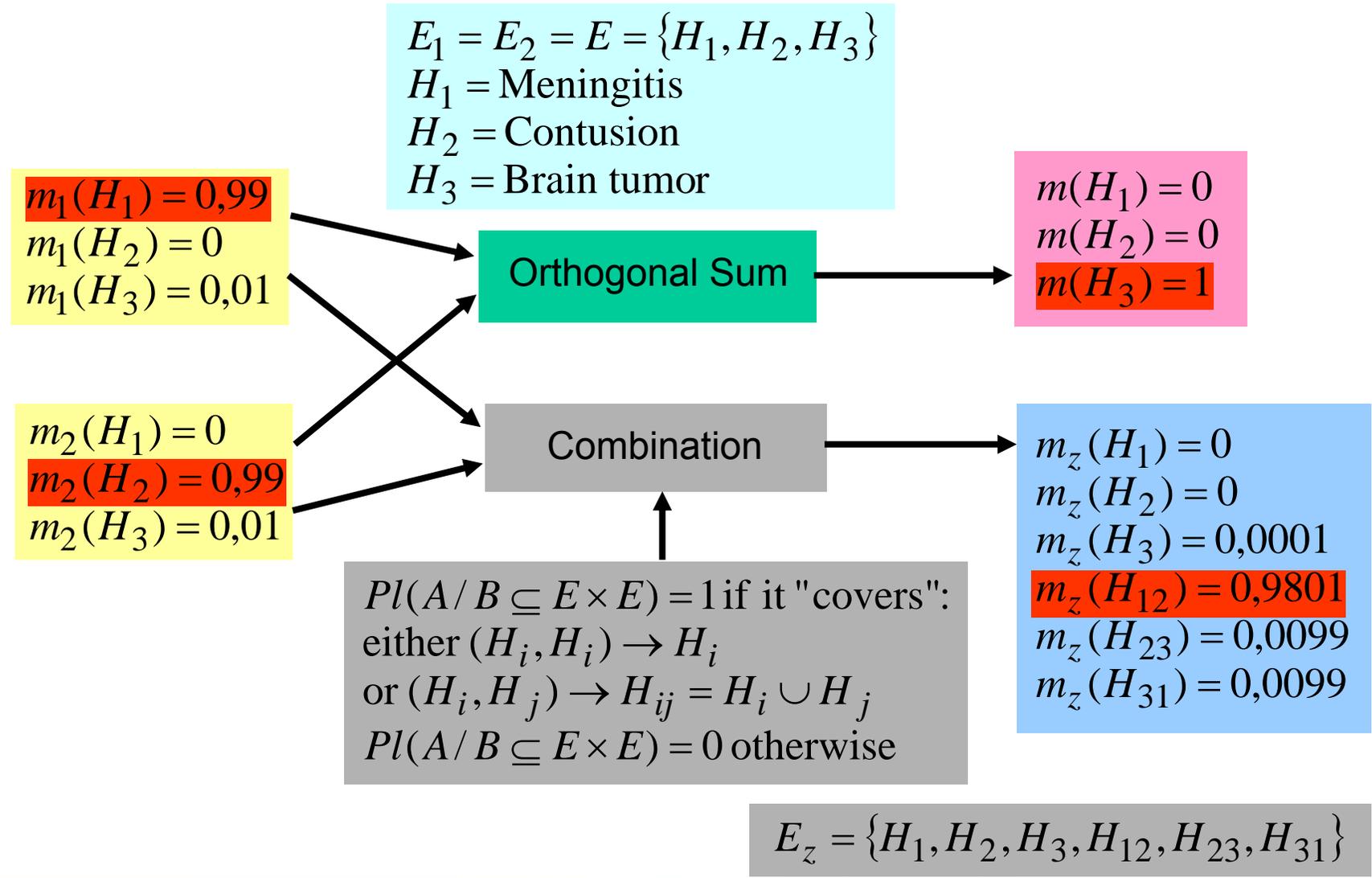
$E_{23} = \{H_2, H_3\}$
 $m_{23}(H_2) = 0,4$
 $m_{23}(H_3) = 0,6$

$E_{31} = \{H_3, H_1\}$
 $m_{31}(H_3) = 0,4$
 $m_{31}(H_1) = 0,6$

S_{ij} : Survey about preferences
 between H_i and H_j
 → Statistics of opinions:
 $P_{ij}(H_i) + P_{ij}(H_j) + P_{ij}(ign.) = 1$

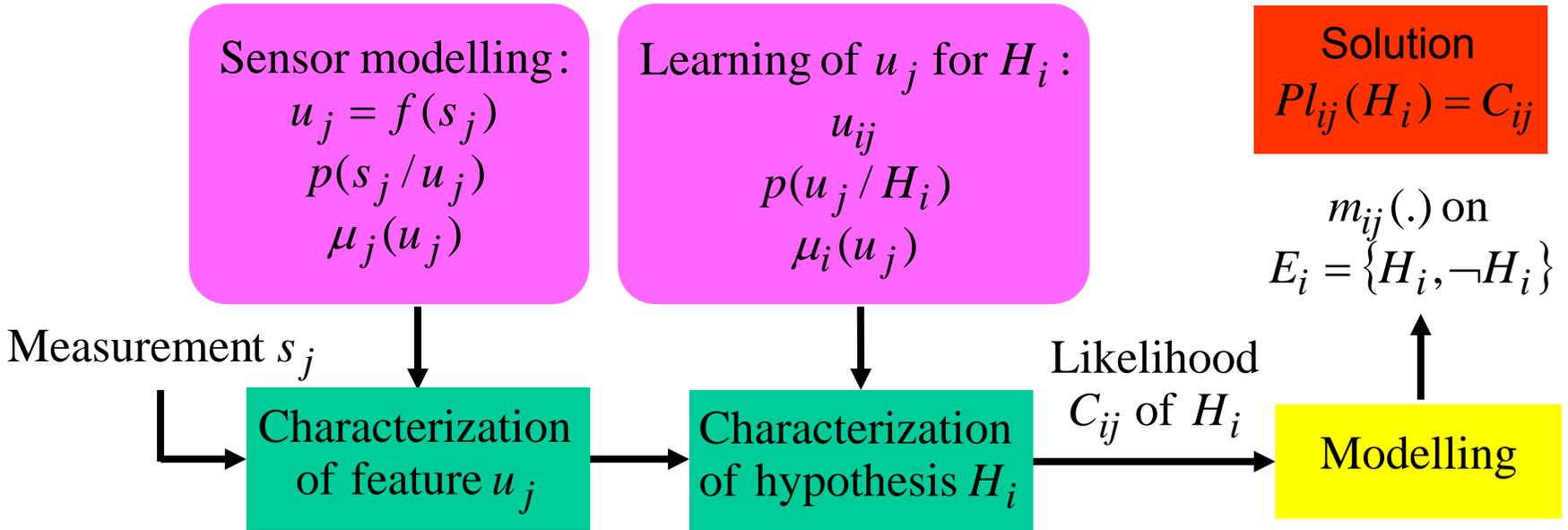


Conflict: Back to Zadeh's Paradox



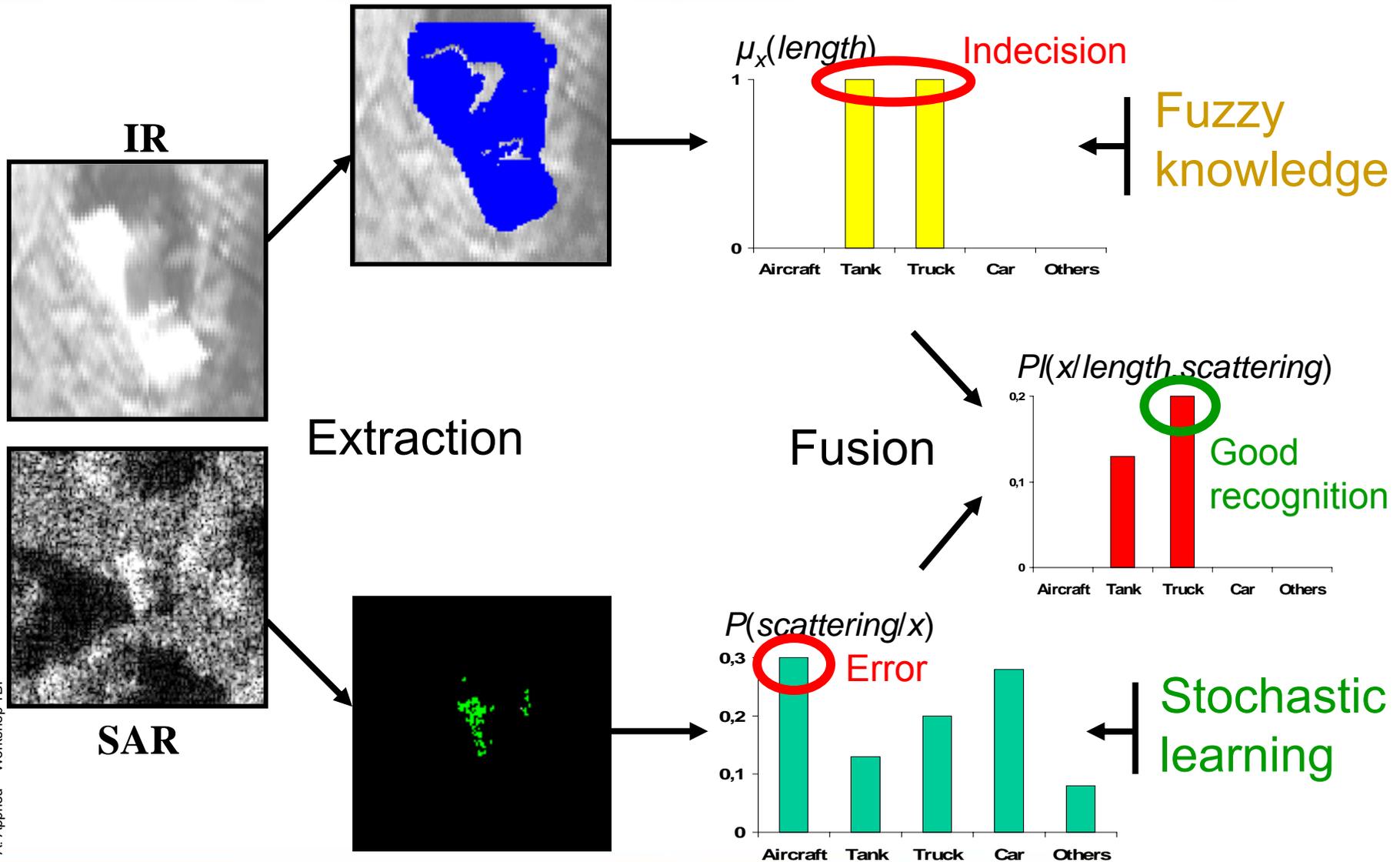
Data Modelling

Principle : separate assessment of each hypothesis or proposition



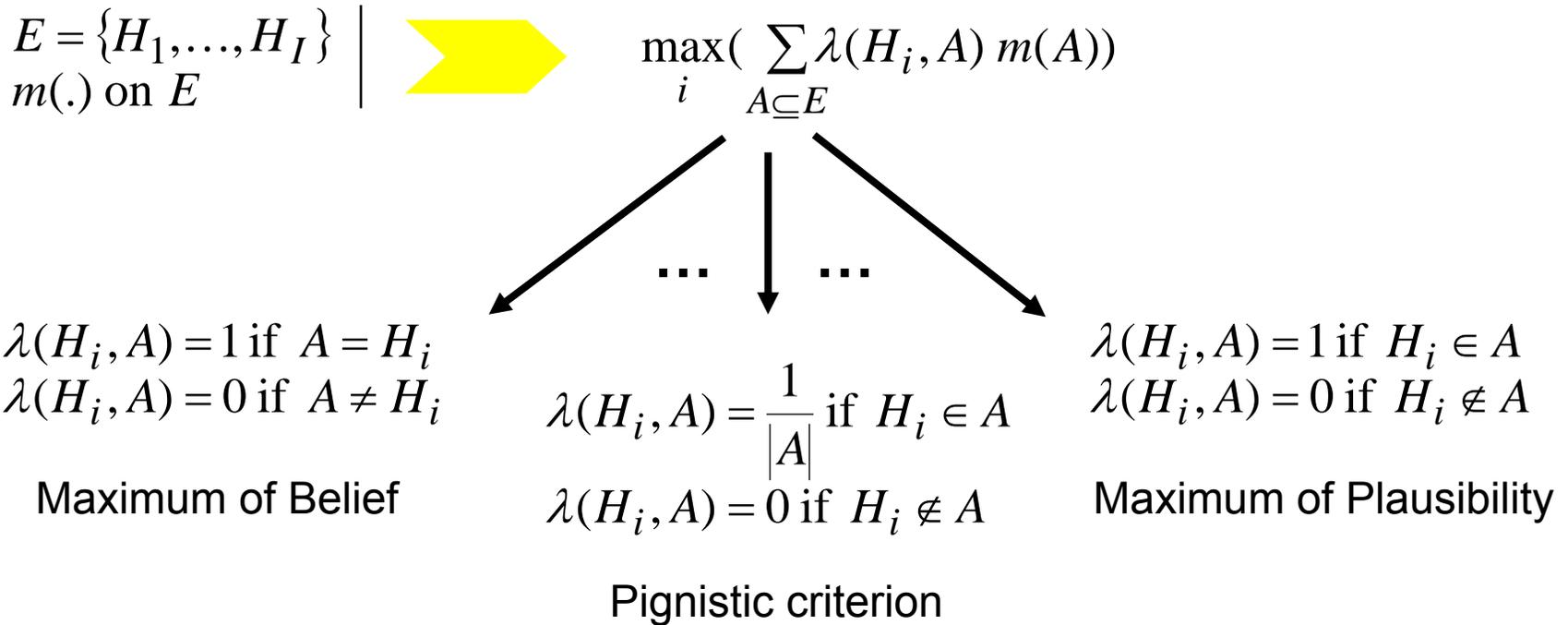
- Potential variety of inputs
- Incomplete information processing - Modularity - Evolutivity
- Reasoning on disparate propositions
- Separate reliability management for each hypothesis
- Contextual data processing: $E_i \rightarrow E_F = \{F, \neg F\}$

Image Fusion for Aerial Recognition



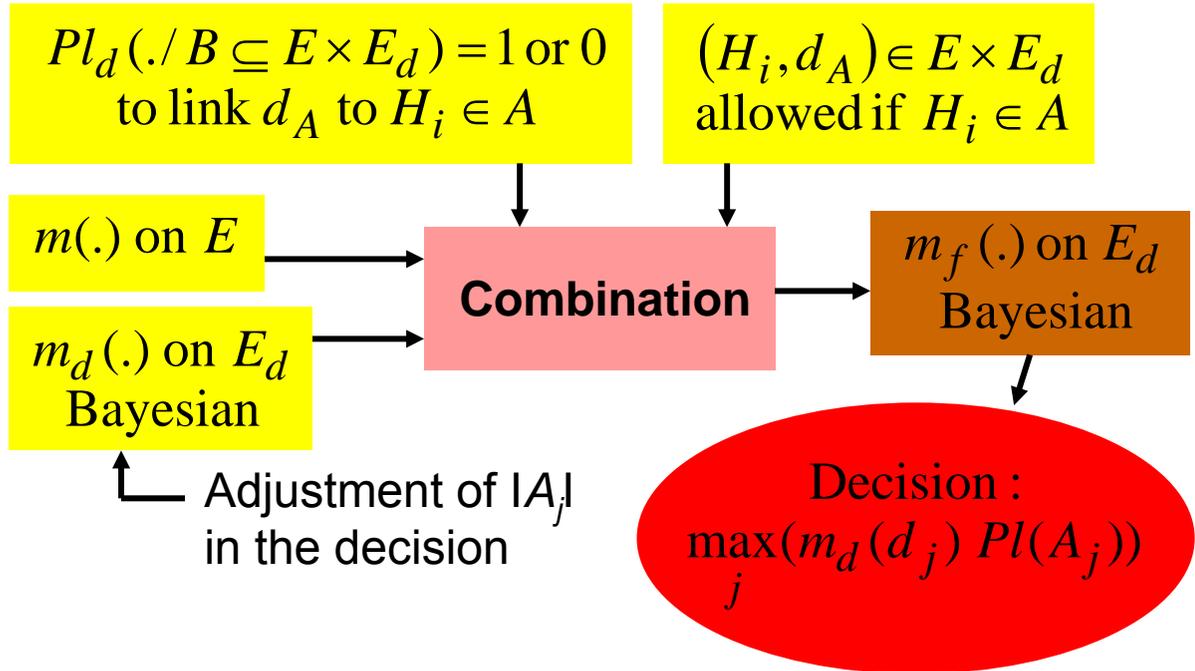
Decision : the Dilemma

Choice of the most likely hypothesis



Decision : Set of the most Likely Hypotheses

$E = \{H_1, \dots, H_I\}$
 $E_d = \{d_1, \dots, d_D\}$
 $H_i = \text{Hypothesis}$
 $d_j = \text{Choice of } A_j \subseteq E$



- Set of hypotheses that includes most likely the right one (\neq set of the best hypotheses considered separately)
- Adjustable compromise between likelihood and precision
- Ambiguities :
 - Parametric adjustment
 - Use of a secondary criterion :
 $\min_j \{m_d(d_{j'} / A_{j'} = \neg A_j) Pl(\neg A_j)\}$

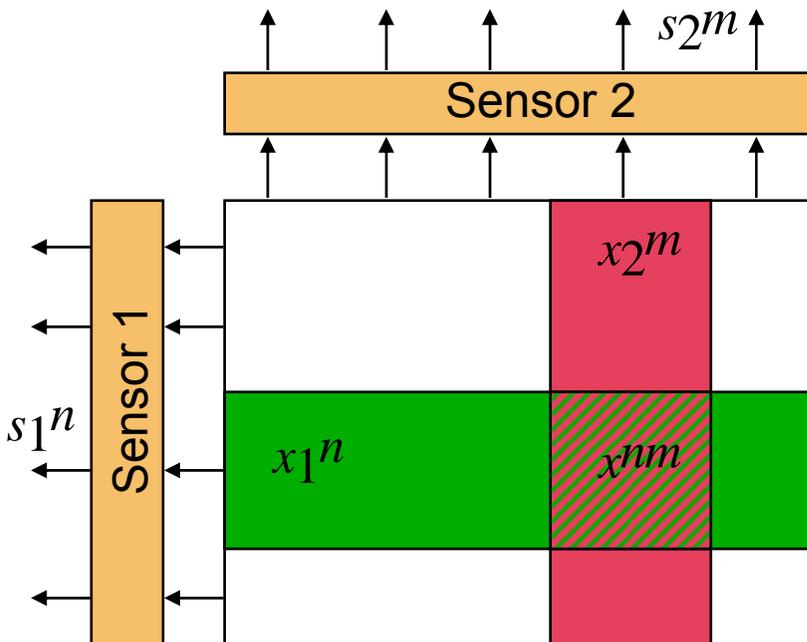
A Few Didactic Examples

$m(H_1)$	0,2	0,1	0,4
$m(H_2)$	0,1	0	0
$m(H_3)$	0,3	0,3	0
$m(H_1 \cup H_2)$	0,2	0,5	0
$m(H_2 \cup H_3)$	0,1	0,1	0,6
$m(E)$	0,1	0	0
Solution(s) with $ \cdot =1$	H_1, H_2, H_3	H_1, H_2	H_2, H_3
Solution(s) with $ \cdot =2$	$H_1 \cup H_3$	$H_1 \cup H_3$	$H_1 \cup H_2, H_1 \cup H_3$
Secondary criterion	H_3	H_1	H_2, H_3
Pignistic criterion	H_3	H_1, H_3	H_1

Ambiguous Observation Matching

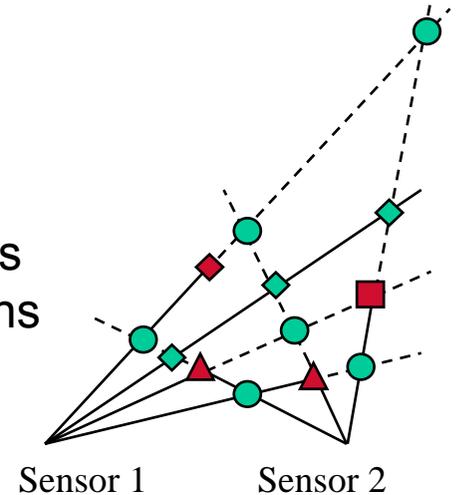
Orthogonal spatial resolutions :

- Localization
- Discrimination of multiple targets



Difficulties :

- Ghosts
- False Alarms
- Hidden targets
- Non-Detections



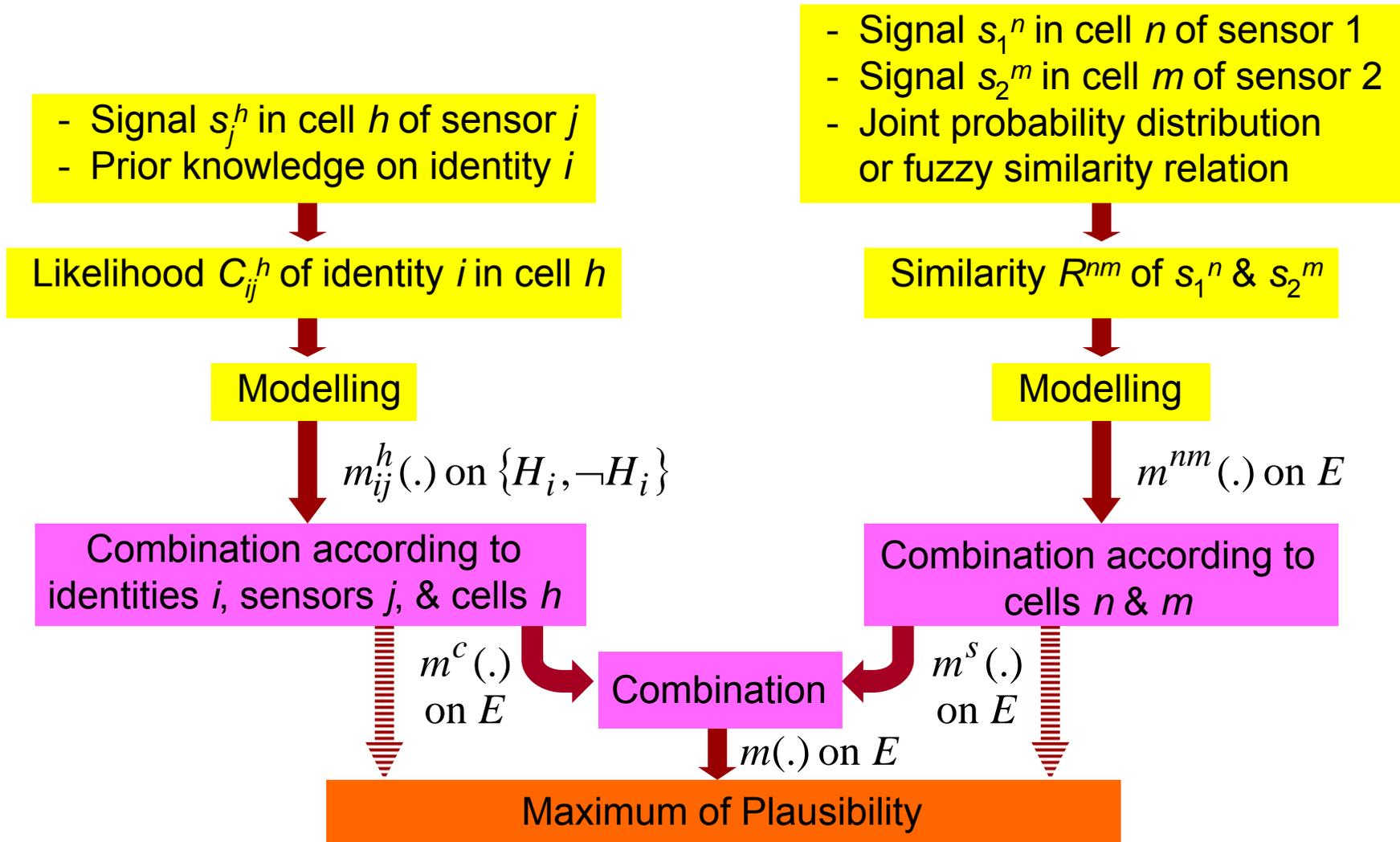
Formulation :

Look for the most likely singleton in the set E of identity distributions over cell intersections

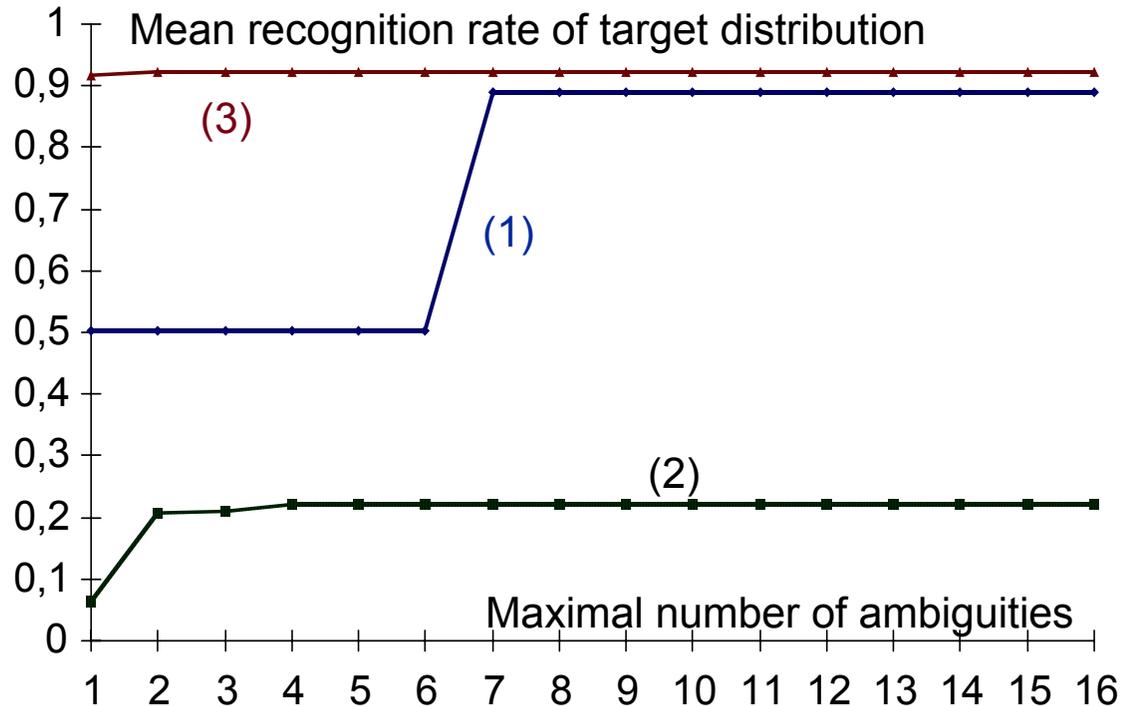
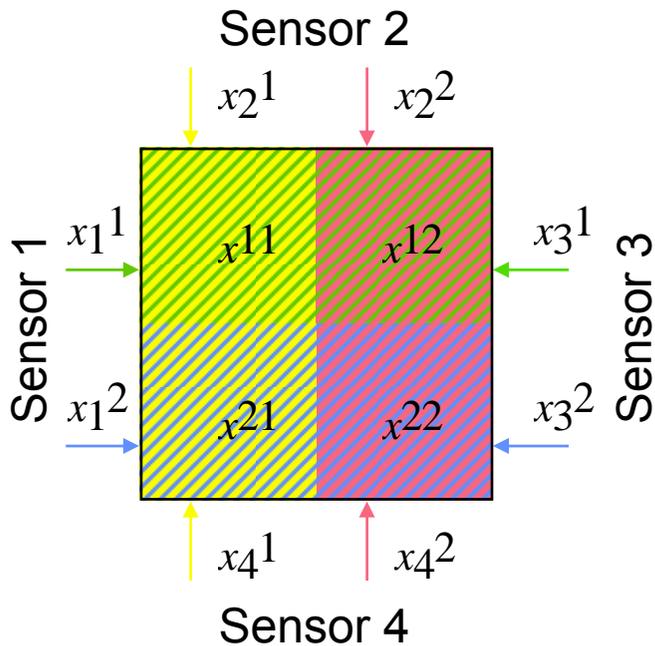


Simultaneous detection, localization, counting, identification of all targets

Matching Process



Application to Detection

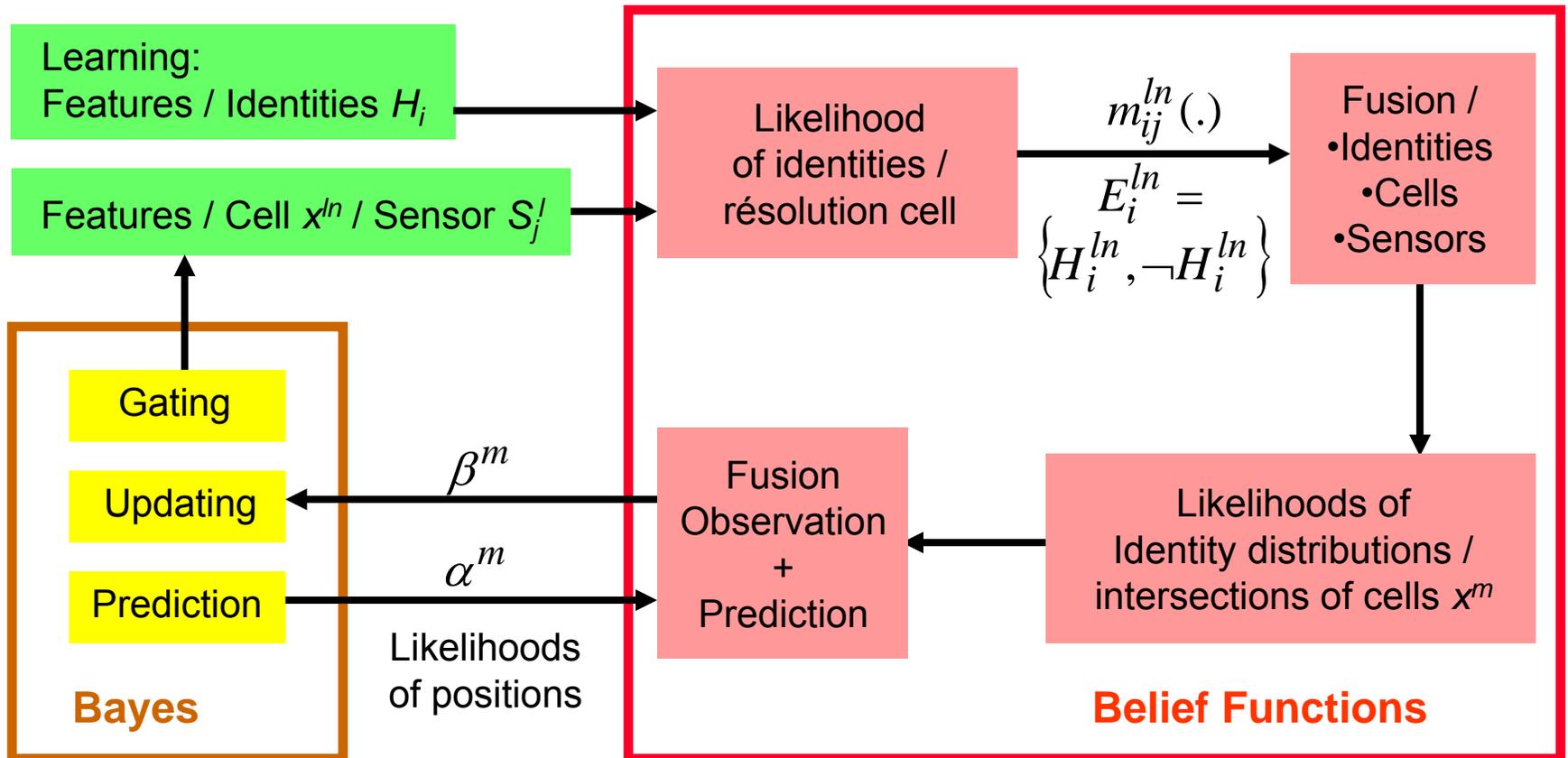


- Statistical learning of signals with and without target
- Fuzzy similarity relation between signals of sensors looking at a same target

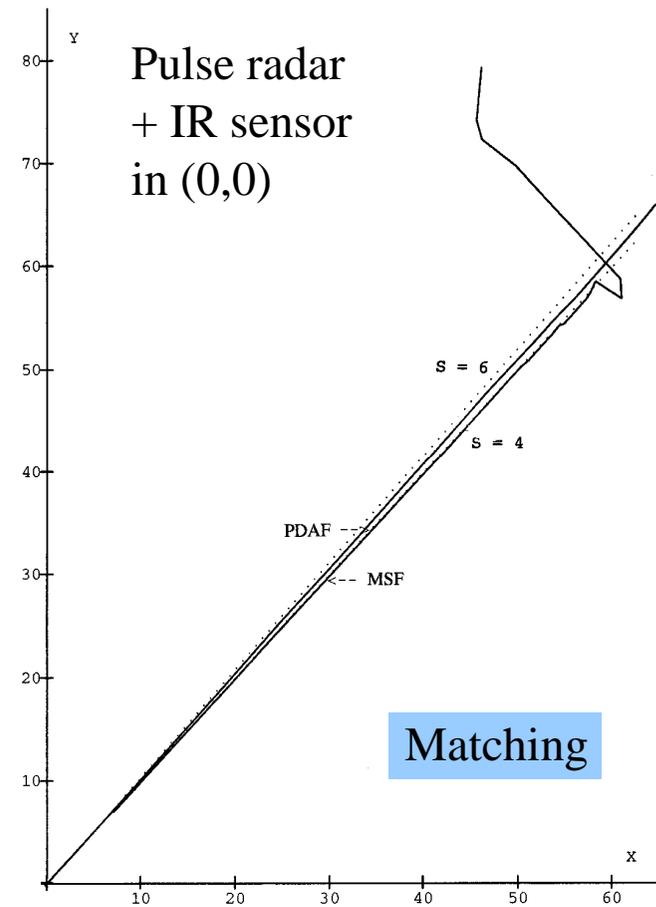
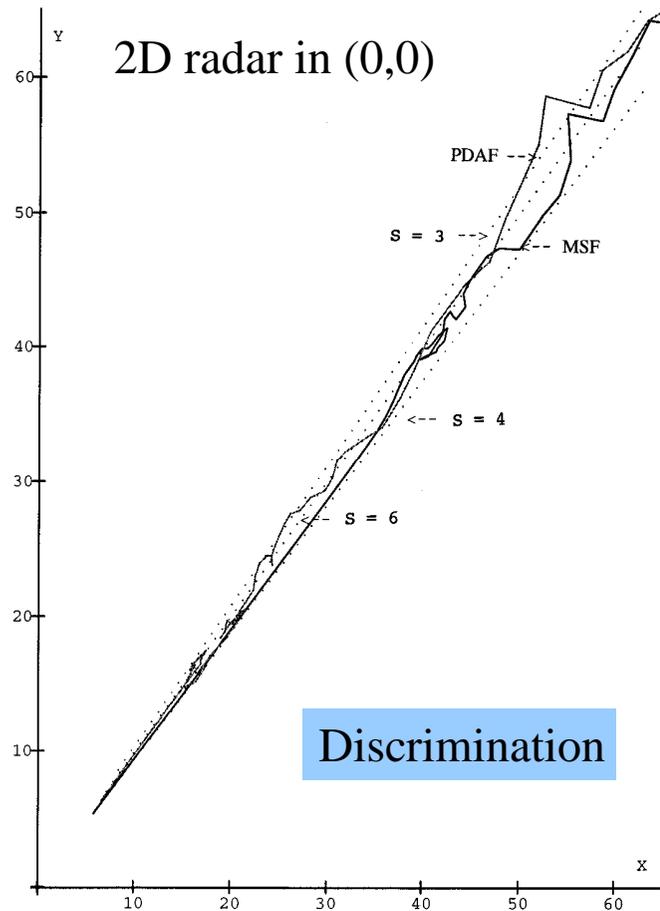
- (1) Classification criterion
- (2) Similarity criterion
- (3) Global criterion

Tracking in Dense Environment

A global approach: Multiple Signal Filter (MSF)



Examples



Signals:

- $N(0,1)$ No target in the cell
- $N(S,1)$ Target level S in the cell

- Reliable statistical learning
- Initialization error only
- Tracking of target $S=4$

Concluding Remarks

**Collection of coherent operators
that meets emerging fusion needs**

- Independent interpretation of heterogeneous data in a same process
- Integration of contextual observations
- Reliability management
- Management of disparate frames of reference and dependencies
- Conflict and information management
- Ambiguous data matching
- Open decision principles

